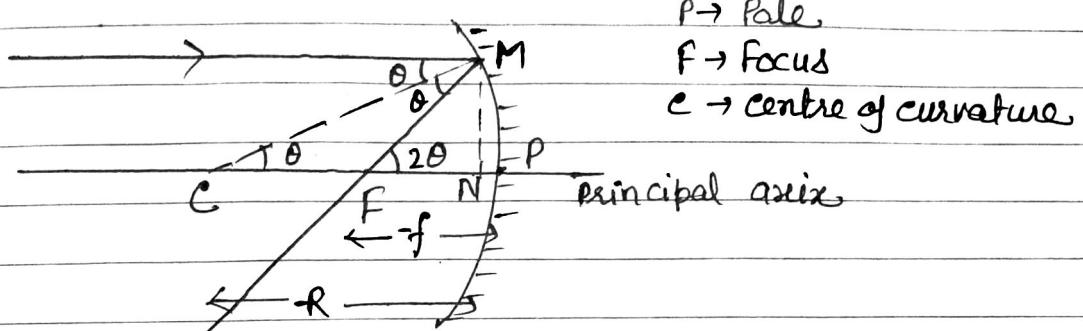


## Derivations of Ray Optics

### 1. Reflection by Spherical Mirrors

- Relation b/w  $f$  and  $R$

Case I - for concave mirror:



In  $\triangle MNC$

$$\tan \theta = \frac{MN}{NC} = \frac{MP}{PC} \quad [ \because P \text{ and } N \text{ are very close} ]$$

for small angle  $\theta$ ,

$$\tan \theta \approx \theta = \frac{MP}{PC} \Rightarrow \theta = \frac{MP}{PC} \quad \text{--- (1)}$$

and in  $\triangle MNF$

$$\tan 2\theta = \frac{MN}{NF} = \frac{MP}{PF} \quad [ \because P \text{ and } N \text{ are close} ]$$

for small angle  $\theta$

$$\tan 2\theta \approx 2\theta = \frac{MP}{PF} \Rightarrow 2\theta = \frac{MP}{PF} \quad \text{--- (2)}$$

From (1) and (2)

$$2 \times \frac{MP}{PC} = \frac{MP}{PF}$$

$$\text{or } 2 \times PF = PC$$

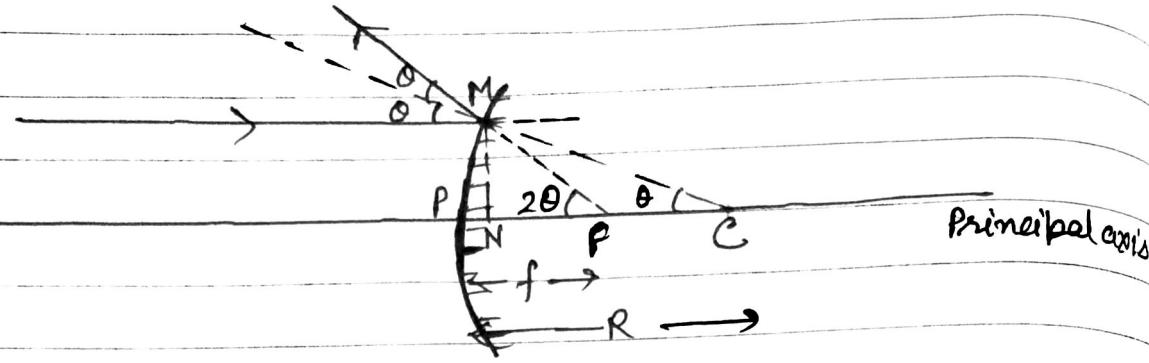
$$\text{or } 2 \times (f+f) = (R)$$

or

$$\boxed{R = 2f} \Rightarrow \boxed{f = \frac{R}{2}}$$

i.e. focal length of a spherical mirror is half of its radius of curvature.

## Case II - for convex mirror



In  $\triangle MNC$

$$\tan \theta \approx \theta = \frac{MN}{NC} = \frac{MP}{PC} \quad \textcircled{1}$$

[P & N are close and theta is very small]

In  $\triangle MNF$

$$\tan 2\theta \approx \theta = \frac{MN}{NF} = \frac{MP}{PF} \quad \textcircled{2}$$

from  $\textcircled{1}$  and  $\textcircled{2}$

$$2 \times \frac{MP}{PF} = \frac{MP}{PC}$$

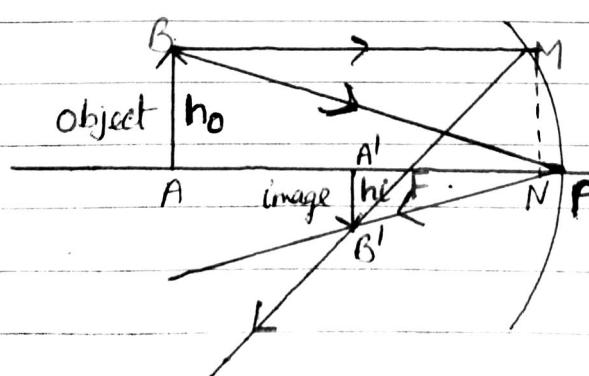
$$\text{or } 2f = R \quad [\text{PF} = +f \text{ and PC} = +R]$$

or

$$f = \frac{R}{2}$$

## 2. Mirror Formula

### Case I For concave mirror (Real Image)



$AB$  = Object,  $A'B'$  = Image

$PA' = -u'$        $PA = -u$

$PF = -f$

N and P are very close

(\* We can take any case of image formation.)

$\triangle ABP$  and  $\triangle A'B'P$  are similar  $\Delta's$ , so,

$$\frac{A'B'}{AB} = \frac{PA'}{PA} \quad \text{--- (1)}$$

$\triangle A'B'F$  and  $\triangle MNF$  are similar  $\Delta's$ , so,

$$\frac{A'B'}{MN} = \frac{FA'}{NF}$$

but  $P$  and  $N$  points are close so  $N \rightarrow P$ , then

$$\frac{A'B'}{MN} = \frac{FA'}{PF} = \frac{PA' - PF}{PF} \quad \therefore \quad [\because FA' = PA' - PF]$$

As  $MN = AB$

$$\frac{A'B'}{AB} = \frac{PA' - PF}{PF} \quad \text{--- (2)}$$

From (1) and (2)

$$\frac{PA'}{PA} = \frac{PA' - PF}{PF}$$

put the values

$$\frac{-v}{fu} = \frac{-v - (-f)}{-f}$$

or  $-vf = -uv + uf$

divide both sides by  $uvf$

$$\frac{-vf}{uvf} = \frac{-uv}{uvf} + \frac{uf}{uvf}$$

$$\text{or } -\frac{1}{u} = -\frac{1}{v} + \frac{1}{f}$$

$$\boxed{\frac{1}{f} = \frac{1}{v} + \frac{1}{u}}$$

Magnification ( $m$ ): Ratio of height of image to height of object.

$\triangle A'BP$  and  $\triangle A'B'P$  are similar  $\Delta$ 's.

$$\frac{A'B'}{AB} = \frac{PA'}{PA}$$

$$\frac{-h_I}{h_o} = \frac{-v}{u}$$

$$\frac{-h_I}{h_o} = \frac{-v}{u}$$

$$\begin{cases} A'B' = -h_I, AB = h_o \\ PA' = -v, PA = -u \end{cases}$$

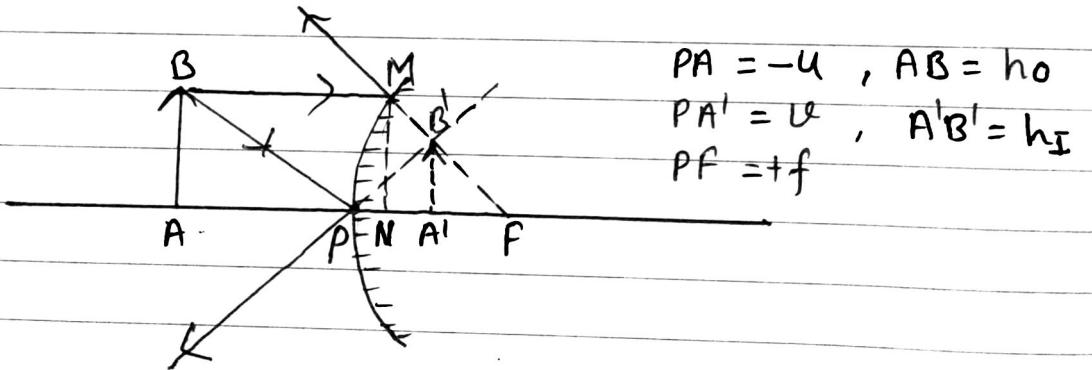
or

$$\frac{h_I}{h_o} = \frac{-v}{u}$$

or

$$m = \frac{h_I}{h_o} = \frac{-v}{u}$$

Case II By convex mirror



$\triangle A'BP$  and  $\triangle A'B'P$  are similar

$$\frac{A'B'}{AB} = \frac{PA'}{PA} \quad \text{--- (1)}$$

$\triangle MNF$  and  $\triangle A'B'F$  are similar and  $MN = AB$   
also  $N \rightarrow P$  as  $N$  &  $P$  are close, then

$$\frac{A'B'}{MN} = \frac{A'B'}{AB} = \frac{A'F}{PF}$$

$$\text{or } \frac{A'B'}{AB} = \frac{PF - PA'}{PF} \quad \text{--- (2)}$$

$$(A'F = PF - PA')$$

From ① and ②

$$\frac{PA'}{PA} = \frac{PF - PA'}{PF}$$

$$\frac{v}{-u} = \frac{f - v}{f}$$

$$\text{or } vf = -uf + uv$$

divide by  $uvf$

$$\frac{1}{u} = \frac{1}{-v} + \frac{1}{f}$$

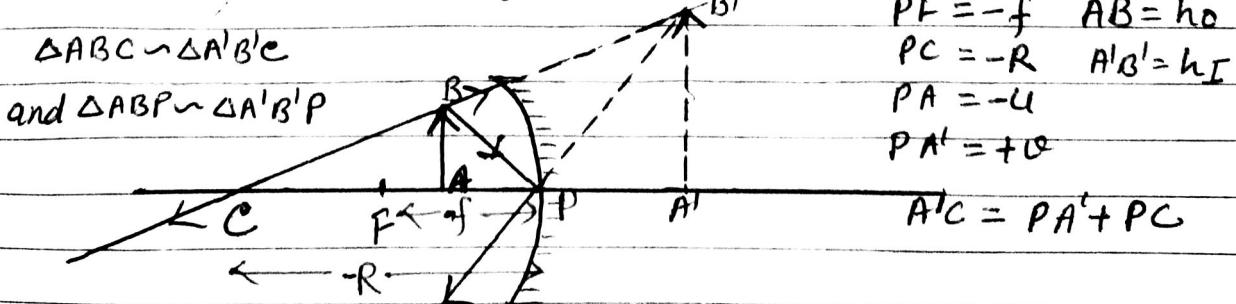
$$\text{or } \boxed{\frac{1}{f} = \frac{1}{v} + \frac{1}{u}}$$

also Magnification ( $m$ ) by  $\triangle ABP$  and  $\triangle A'B'P$

$$\boxed{m = \frac{h_I}{h_o} = -\frac{v}{u}}$$

- \* If  $m = -ve \Rightarrow$  Real and inverted image
- \* If  $m = +ve \Rightarrow$  Virtual and erect image.
- \* If  $m > 1 \Rightarrow$  Image is larger than object ( $h_I > h_o$ )
- \* If  $m < 1 \Rightarrow$  Image is smaller than object ( $h_I < h_o$ )
- \* If  $m = 1 \Rightarrow h_I = h_o$

\* Virtual Image by concave mirror



We can derive same mirror formula for this case also.  
by using similar  $\triangle$ 's.

### 3. Refraction

Relation b/w Real and Apparent depth

From fig

In  $\triangle AOB$

$$\sin i = \frac{AB}{OB}$$

and In  $\triangle AIB$

$$\sin r = \frac{AB}{IB}$$

Now by Snell's law

$$\frac{\sin i}{\sin r} = n_a$$

$$\text{or } n_a = \frac{\sin i}{\sin r} = \frac{AB/OB}{AB/IB}$$

$$\text{or } n_a = \frac{IB}{OB}$$

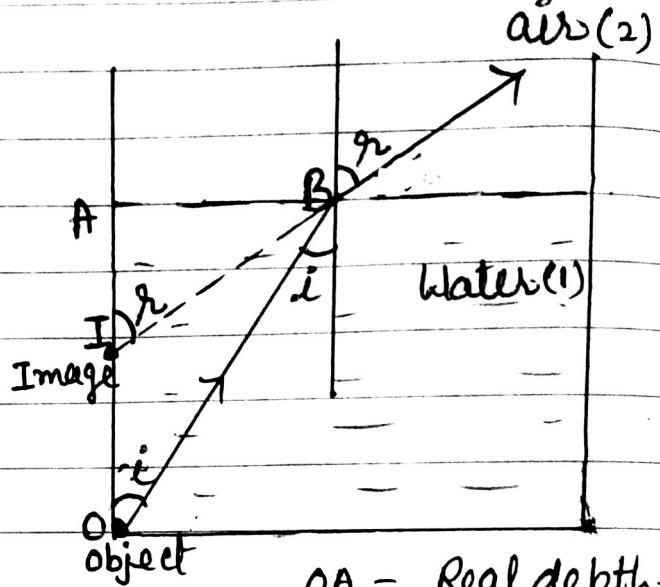
for small angle 'i' and 'r'  $IB = IA$  and  $OB = OA$   
then

$$n_a = \frac{IA}{OA}$$

$$\text{or } n_a = \frac{OA}{IA} = \frac{\text{Real depth}}{\text{App. depth}}$$

$$\text{or } n_2 = \frac{\text{Real depth}}{\text{App. depth}} = \frac{n_1}{n_2}$$

here  $n_2$  is refractive index of denser medium.



$OA$  = Real depth

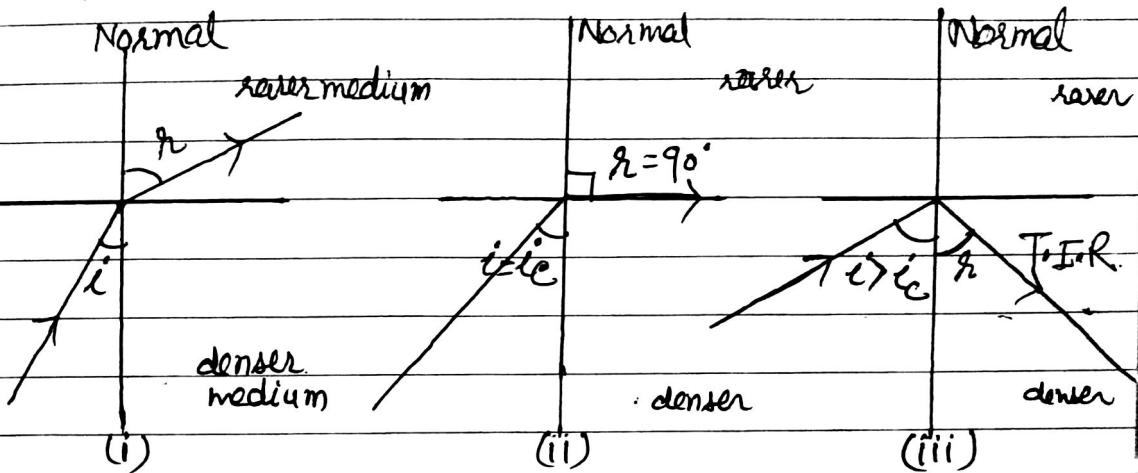
$IA$  = Apparent depth

## Total Internal Reflection

When a ray moves from rarer to denser medium, it moves away from normal. Also  $\angle i \propto \angle r$  i.e. on increasing  $\angle i$ , refraction angle  $\angle r$  also increases.

At a particular value of  $\angle i$ ,  $\angle r$  becomes  $= 90^\circ$ .

This angle of  $\angle i$  is called critical angle  $\angle c$  or  $C$ .



## Relation b/w Refraction Index And critical Angle

From (ii)

$$d\mu_r = \frac{\sin i_c}{\sin 90^\circ} \quad [\text{By Snell's law}]$$

$$\frac{\sin i}{\sin r} = \frac{\sin i_c}{\sin 90^\circ}$$

$$\text{or } d\mu_r = \frac{\sin i_c}{\sin r}$$

$$\text{or } \frac{1}{d\mu_d} = \frac{1}{\sin i_c} \quad [ \because \frac{1}{d\mu_d} = 2^n_1 ]$$

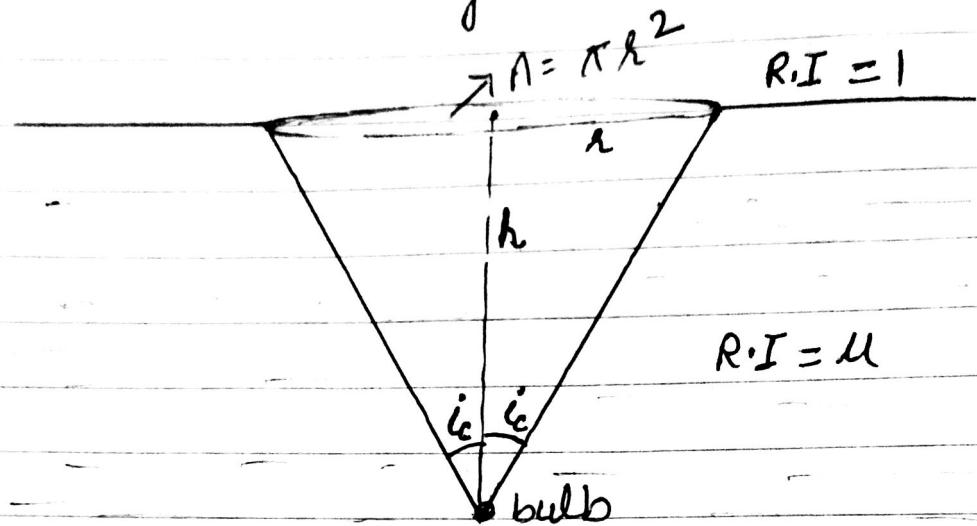
or

$$\boxed{d\mu_d = \frac{1}{\sin i_c} = \frac{1}{\sin C}}$$

or

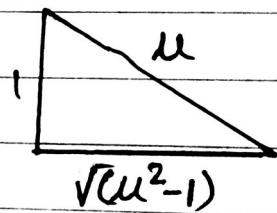
$$\boxed{\sin C = \frac{\text{Velocity of light in denser medium}}{\text{Velocity of light in air}}}$$

\* Area Illuminated By Bulb In Pool (For numericals)



$$\tan i_c = \frac{r}{h} \Rightarrow r = h \cdot \tan i_c$$

$$\sin i_c = \frac{1}{\mu}$$



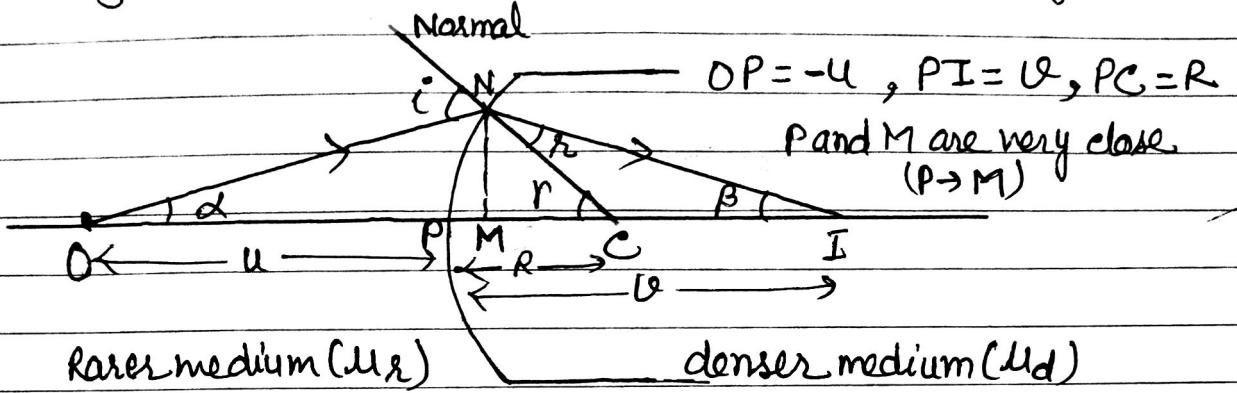
$$\Rightarrow r = \frac{h}{\sqrt{\mu^2 - 1}}$$

$$\text{and Area} = \frac{\pi h^2}{(\mu^2 - 1)} \quad [\text{Area} = \pi r^2]$$

# Refraction at Spherical Surfaces

## I Refraction at a convex spherical surface

(i) Object lie in rarer medium (For Real Image)



In  $\triangle NOC$

$$i = \alpha + r \quad \text{---(1)} \quad [i \text{ is exterior angle}]$$

Similarly in  $\triangle NIC$

$$r = \beta + \gamma \quad [r \text{ is exterior angle}]$$

$$\text{or } \gamma = r - \beta \quad \text{---(2)}$$

Now for small angles  $\alpha$ ,  $\beta$  and  $\gamma$

$$\tan \alpha \approx \alpha = \frac{NM}{OM} = \frac{NM}{OP} \quad [M \text{ & } P \text{ are very close}]$$

$$\tan \beta \approx \beta = \frac{NM}{PI}$$

$$\tan \gamma \approx \gamma = \frac{NM}{PC}$$

Now by Snell's law

$$\frac{\sin i}{\sin r} = \frac{\mu_2}{\mu_1}$$

for small angle of  $i$  and  $r$

$$\mu_1 i = \mu_2 r$$

from (1) and (2) put value of  $i$  and  $r$ .

$$\mu_1 (\alpha + r) = \mu_2 (r - \beta)$$

Now put value of  $\alpha$ ,  $\beta$  and  $\rho$

$$u_1 \left( \frac{NM}{OP} + \frac{NM}{PC} \right) = u_2 \left( \frac{NM}{PC} - \frac{NM}{PI} \right)$$

or  $u_1 \left( \frac{1}{-u} + \frac{1}{R} \right) = u_2 \left( \frac{1}{R} - \frac{1}{v} \right)$

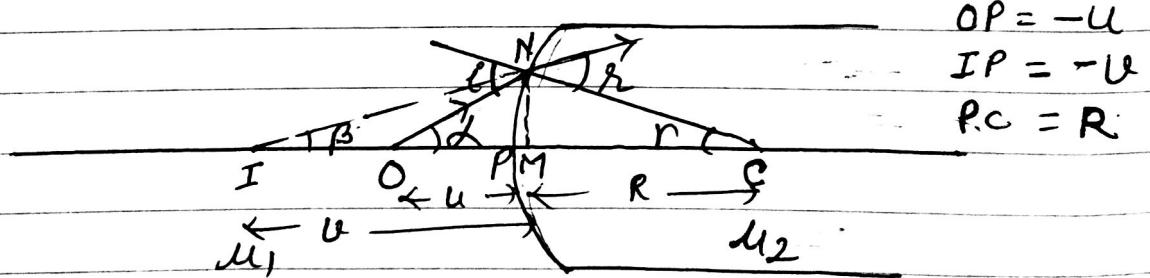
or 
$$\boxed{-\frac{u_1}{u} + \frac{u_2}{v} = \frac{u_2 - u_1}{R}}$$

\* If medium 1 is air,  $u_1=1$  and  $u_2=u$ , then

$$-\frac{1}{u} + \frac{1}{v} = \frac{u-1}{R}$$

or 
$$\boxed{\frac{u}{v} - \frac{1}{u} = \frac{u-1}{R}}$$

(ii) For Virtual Image



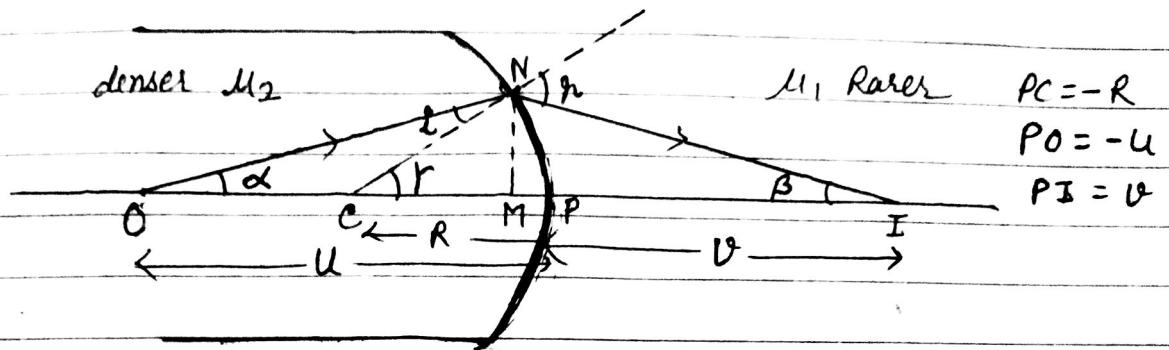
From fig  $i^o = \alpha + \beta$  in  $\triangle NOC$   
and  $\alpha = \beta + r$  in  $\triangle NIC$

-- Same method --

Same formula we get i.e

$$-\frac{u_1}{u} + \frac{u_2}{v} = \frac{u_2 - u_1}{R}$$

(iii) Object lie in the denser medium

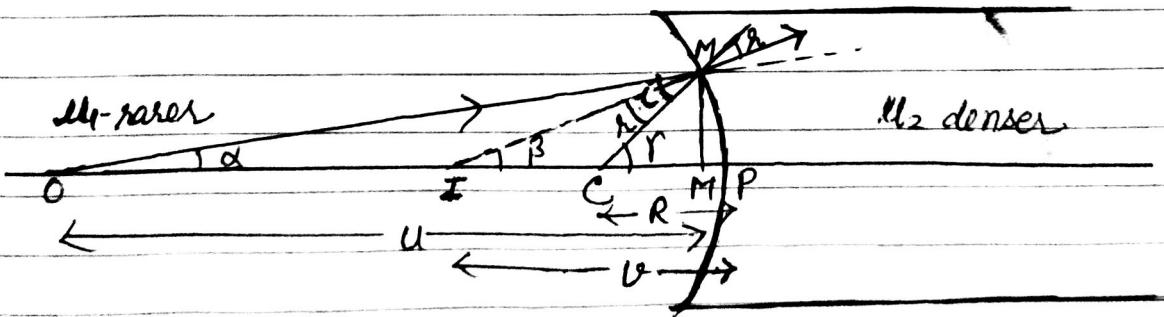


From fig.

$$r = \alpha + i \Rightarrow i = r - \alpha \quad [\text{In } \triangle ONC]$$

$$\alpha = \beta + r \quad [\text{In } \triangle CNI]$$

## 2. Refraction at concave surface



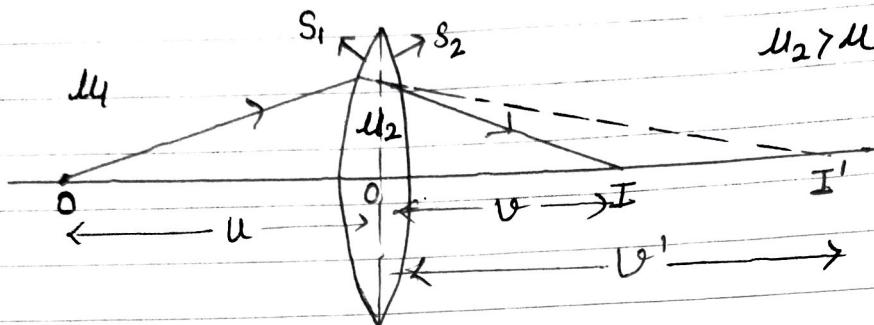
From fig.

$$i = r - \alpha \quad [\text{In } \triangle MOP]$$

$$\alpha = r - \beta \quad [\text{In } \triangle MSC]$$

# Lens Maker's Formula

For convex lens,



$u_2 > u_1$ ,  $u_2 \rightarrow$  of lens  
 $u_1 \rightarrow$  of medium

For refraction at surface  $S_1$ ,

$$-\frac{u_1}{u} + \frac{u_2}{v'} = \frac{u_2 - u_1}{R_1} \quad \text{--- (1)}$$

For surface  $S_2$

$$-\frac{u_2}{v'} + \frac{u_1}{v} = \frac{u_1 - u_2}{R_2} \quad \text{--- (2)}$$

on adding (1) and (2)

$$\frac{u_1}{v} - \frac{u_1}{u} = \frac{u_1 - u_2}{R_2} + \frac{u_2 - u_1}{R_1}$$

$$\text{or } u_1 \left[ \frac{1}{v} - \frac{1}{u} \right] = (u_2 - u_1) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$\text{or } \frac{1}{v} - \frac{1}{u} = \frac{u_2 - u_1}{u_1} \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$\text{or } \frac{1}{v} - \frac{1}{u} = \left( \frac{u_2}{u_1} - 1 \right) \left( \frac{1}{R_1} - \frac{1}{R_2} \right) \quad \text{--- (3)}$$

If object is placed at  $\infty$  ( $u = \infty$ ),  $v = f$

$$\Rightarrow \frac{1}{f} - \frac{1}{\infty} = \left( \frac{\mu_2}{\mu_1} - 1 \right) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

or

$$\frac{1}{f} = (\mu_2 - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\text{Eq } 4 \quad \frac{\mu_2}{\mu_1} = \frac{\text{lens}}{\text{medium}}$$

This is the lens maker's formula.

\* When lens is placed in air,  $\mu_1 = 1$ ,  $\mu_2 = \mu$ , then

$$\frac{1}{f} = (\mu - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

\* Focal length in diff medium

$$f_{\text{med.}} = \frac{\mu_e - \mu_m}{(\mu_e - 1)\mu_m}$$

here,

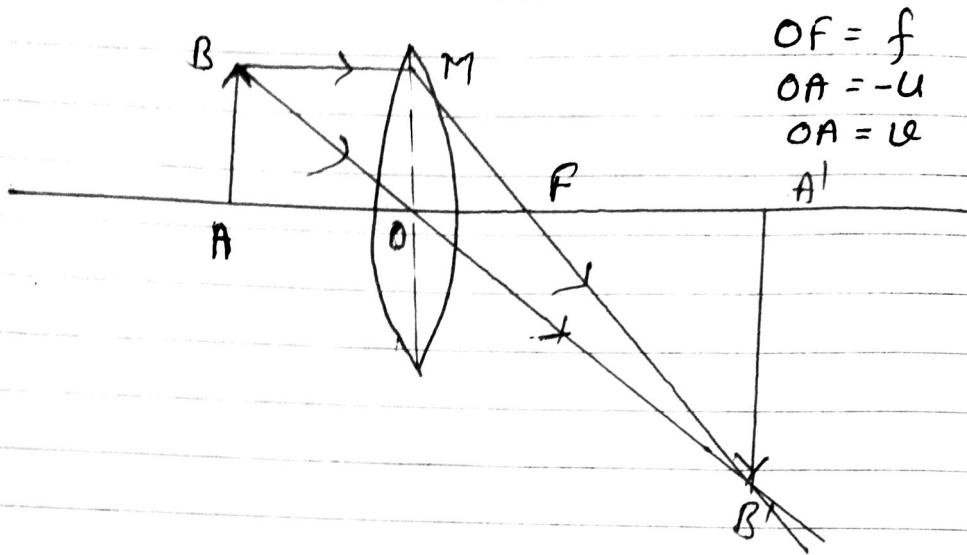
$\mu_e \rightarrow$  R.I of lens

$\mu_m \rightarrow$  R.I of med.

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

This is the lens formula.

# Derivation of Lens Formula



In  $\triangle ABO$  and  $A'B'O$

$$\frac{AB}{A'B'} = \frac{OA}{OA'} - \textcircled{1} \quad [\triangle ABO \sim \triangle A'B'O]$$

In  $\triangle MOF$  and  $A'B'F$

$$\frac{MO}{A'B'} = \frac{OF}{FA'} \quad [\text{similar } \triangle's]$$

but  $MO = AB$ , then

$$\frac{AB}{A'B'} = \frac{OF}{FA'} - \textcircled{2}$$

from (1) and (2)

$$\frac{OA}{OA'} = \frac{OF}{FA'} = \frac{OF}{OA' - OF}$$

$$\text{or } \frac{-u}{v} = \frac{f}{v-f}$$

or,

$$-uv + uf = vf$$

dividing by  $uvf$

$$\frac{-u/v}{uvf} + \frac{u/f}{uvf} = \frac{v/f}{uvf}$$

or  $\frac{1}{-f} + \frac{1}{v} = \frac{1}{u}$

or  $\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$

This is the lens formula and true for every case of convex and concave lens.

Linear Magnification ( $m$ ) The ratio of size of image to the size of object is called linear magnification.

$$m = \frac{h_I}{h_o} = \frac{\text{height of image}}{\text{height of object}}$$

$\triangle AOB \sim \triangle A'OB'$

$$\frac{A'B'}{AB} = \frac{OA'}{OA}$$

$$-\frac{h_I}{h_o} = +\frac{v}{u}$$

or  $m = \frac{h_I}{h_o} = \frac{v}{u}$

\*  $m = \frac{v}{u} = \frac{f}{f+u} = \frac{f-u}{f}$   $\left[ \because \frac{1}{v} = \frac{1}{f} + \frac{1}{u}, \frac{1}{u} = \frac{1}{f} - \frac{1}{v} \right]$

$|m| > 1 \Rightarrow$  larger image

$|m| < 1 \Rightarrow$  smaller image

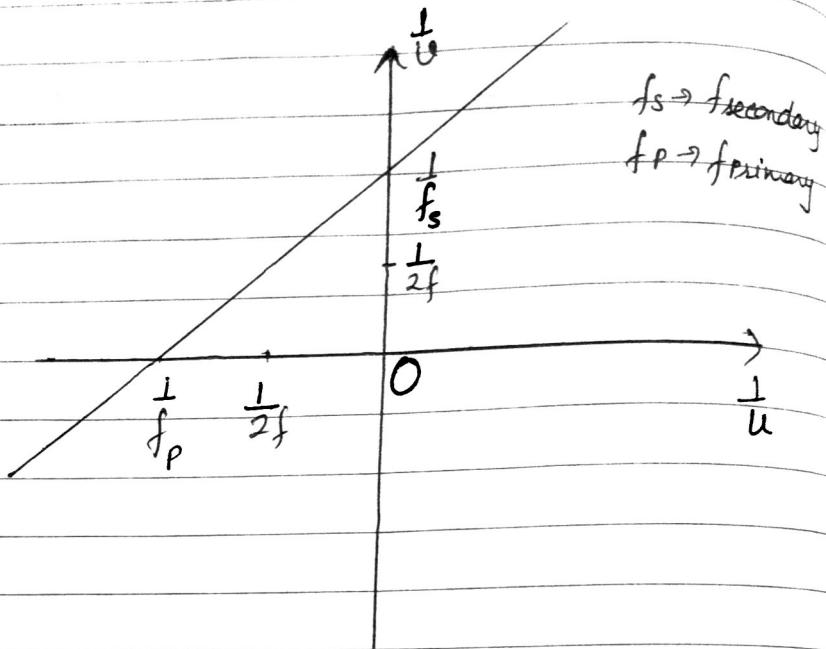
$|m| = 1 \Rightarrow$  same size image

$m$  is +ve  $\Rightarrow$  virtual and erect image

$m$  is -ve  $\Rightarrow$  real and inverted image

Graph b/w  $\frac{1}{v}$  and  $\frac{1}{u}$  for convex lens

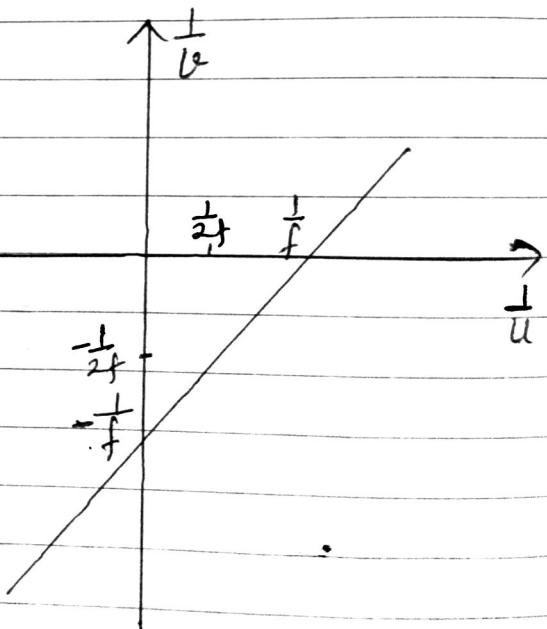
$$\begin{aligned}\frac{1}{v} - \frac{1}{u} &= \frac{1}{f} \\ \Rightarrow y - x &= c \\ \Rightarrow y &= x + c\end{aligned}$$



For concave lens

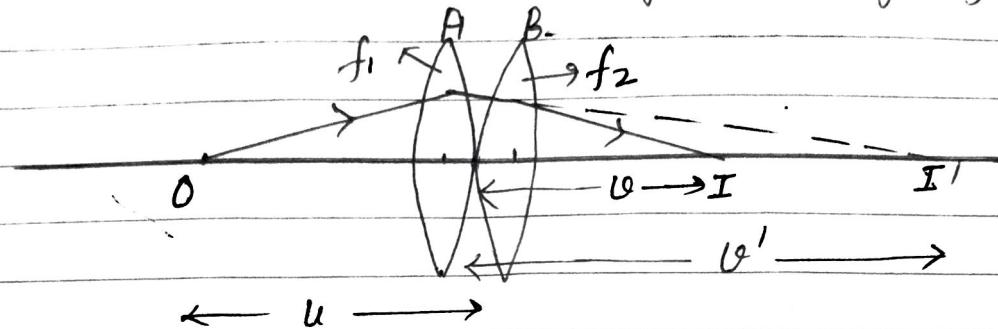
$$\begin{aligned}y - x &= -c \\ \Rightarrow y &= x - c\end{aligned}$$

If forms always  
virtual and erect image.  
Which is diminished of  
real image.



combination of thin lenses in contact

consider two lenses A and B of focal length  $f_1$  and  $f_2$ .



For image formed by lens 'A'

$$\frac{1}{f_1} = \frac{1}{v'} - \frac{1}{u} \quad \text{--- (1)}$$

For lens 'B'

$$\frac{1}{f_2} = \frac{1}{v} - \frac{1}{v'} \quad \text{--- (2)}$$

Adding (1) and (2)

$$\frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{v} - \frac{1}{u}$$

or  $\frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{f} \quad \left[ \because \frac{1}{v} - \frac{1}{u} = \frac{1}{f} \right]$

For several thin lenses

$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3} + \dots$$

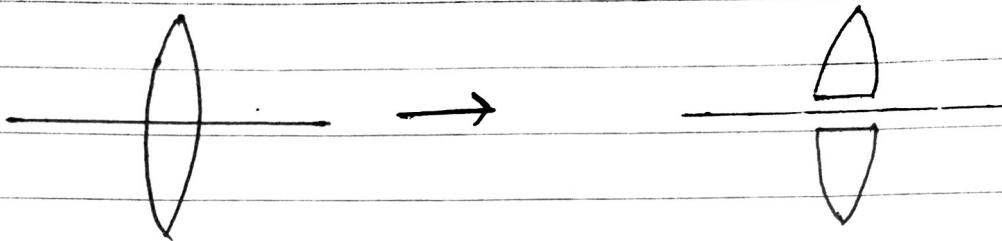
and power

$$P = P_1 + P_2 + P_3 + \dots$$

\* combination of lenses improve magnification

$$m = m_1 m_2 m_3 \dots$$

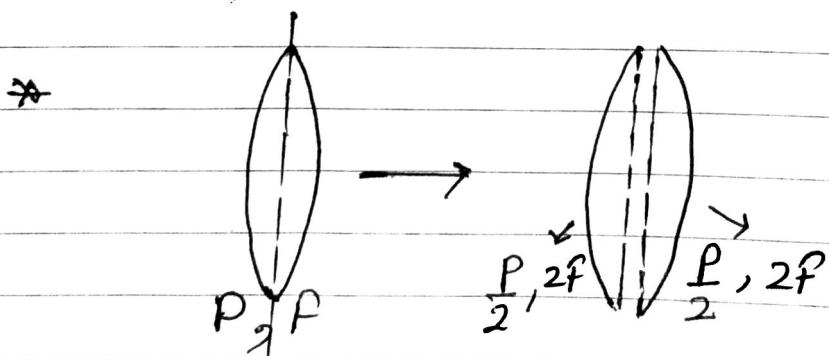
\* cutting of lens



- Power and focal length are unchanged
- Intensity become half as

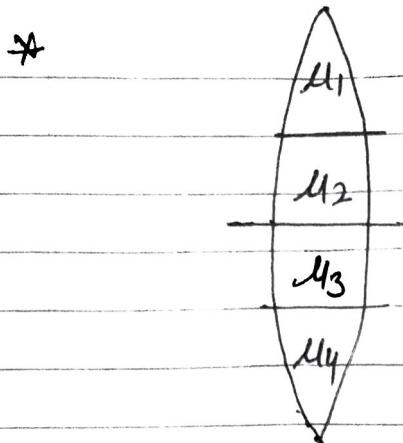
Intensity  $\propto$  Aperture area

\* + =  $2P, \frac{F}{2}$

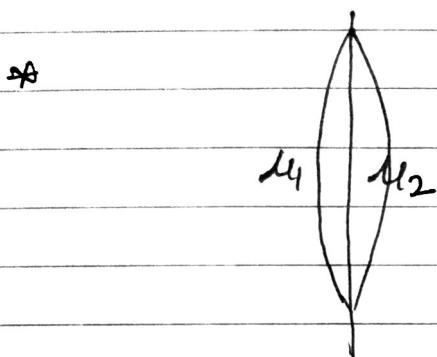


Intensity is unchanged as aperture is unaffected

\* + =  $2P$



- Four focal lengths
- Four Images



- 1 object
- 1 focal length
- 1 Image

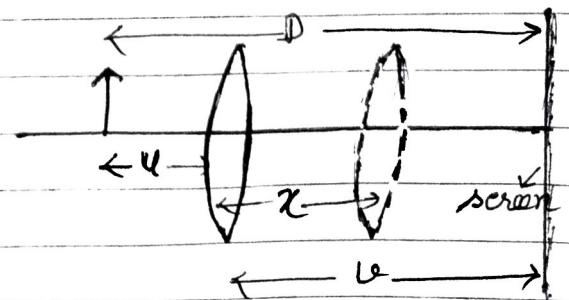
#### \* Silvering of a lens / lens mirror combination

$$\frac{1}{f_{eq}} = \frac{1}{f_l} + \frac{1}{f_m}$$

system      lens      mirror      Equivalent mirror

#### \* Determination of focal length of convex lens by displacement method -

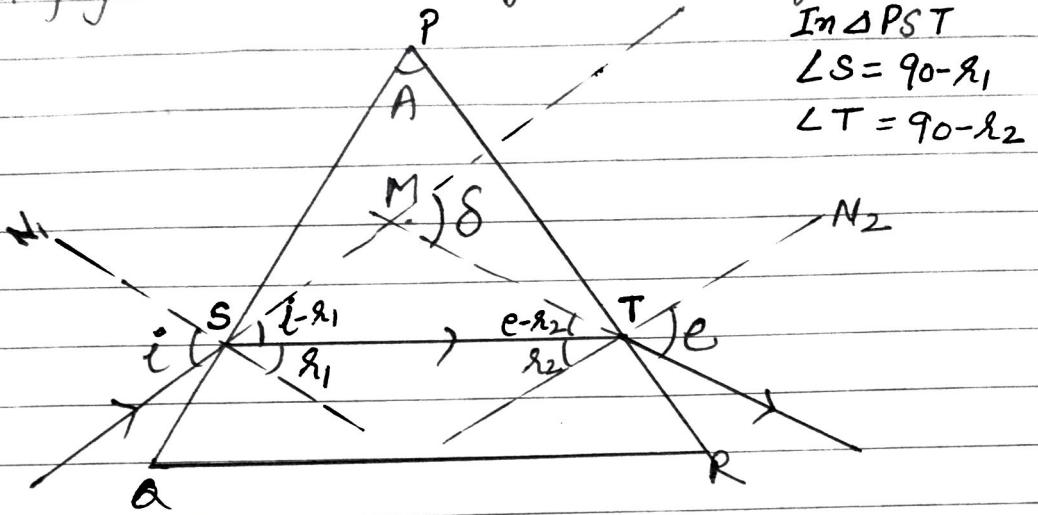
$$f = \frac{D^2 - x^2}{4D}$$



## Refraction by Prism

### Deviation Produced by a prism

In fig -  $A \rightarrow$  Prism angle,  $\delta \rightarrow$  Angle of deviation



$$\begin{aligned} \text{In } \triangle PST \\ \angle S = 90 - r_1 \\ \angle T = 90 - r_2 \end{aligned}$$

From fig.

In  $\triangle PST$

$$A + \angle S + \angle T = 180$$

$$A + (90 - r_1) + (90 - r_2) = 180$$

$$\text{or } A = r_1 + r_2 \quad \text{--- (1)}$$

In  $\triangle MST$

$$\delta = (i - r_1) + (e - r_2) \quad [\delta \text{ is exterior angle}]$$

$$\text{or } \delta = i + e - (r_1 + r_2)$$

$$\text{or } \boxed{\delta = i + e - A} \quad [ \because r_1 + r_2 = A, \text{ from eqn (1)} ]$$

\*  $\delta$  depends upon  $i$

minimum Deviation - At minimum deviation

$$\delta = \delta_m, \quad i = e$$

$$\text{i.e. } r_1 = r_2 \Rightarrow \delta = \frac{A}{2} \quad [\text{from eqn (1)}]$$

$$\text{and } \delta_m = i + e - A = 2i - A$$

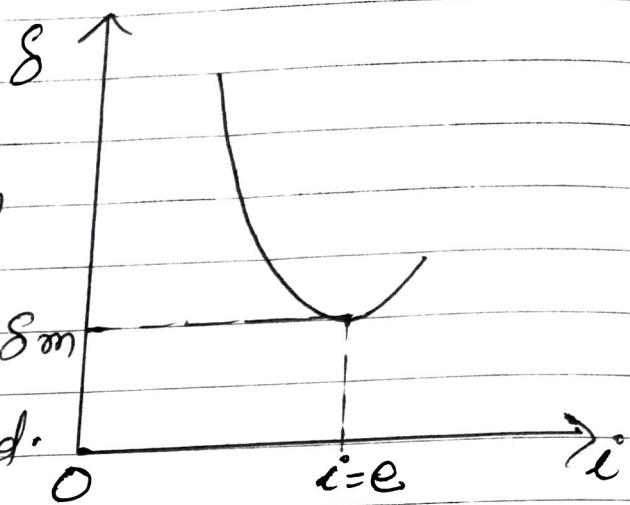
$$\boxed{\delta_m = 2i - A} \quad \text{--- (2)}$$

Graph b/w  $\delta$  and  $i^\circ$

Initially  
 $i^\circ \uparrow, \delta \downarrow$

at  $i^\circ = e$ ,  $\delta$  becomes  $\delta_m$   
then,  $i^\circ \uparrow, \delta \uparrow$

\*  $\delta$  remain same if  
 $i^\circ$  and  $e$  are interchanged.



Expression for Refractive Index of prism -

By snell's law

$$\frac{\sin i}{\sin r} = \mu_2$$

from eqn ③  $\delta_m = 2i - A$

$$i = \frac{\delta_m + A}{2}$$

and from eqn ①  $r_1 + r_2 = A$ , for  $r_1 = r_2$

$$2r = A \Rightarrow r = \frac{A}{2}$$

So

$$\mu_2 = \frac{\sin i}{\sin r} = \frac{\sin(\delta_m + A)}{\sin \frac{A}{2}}$$

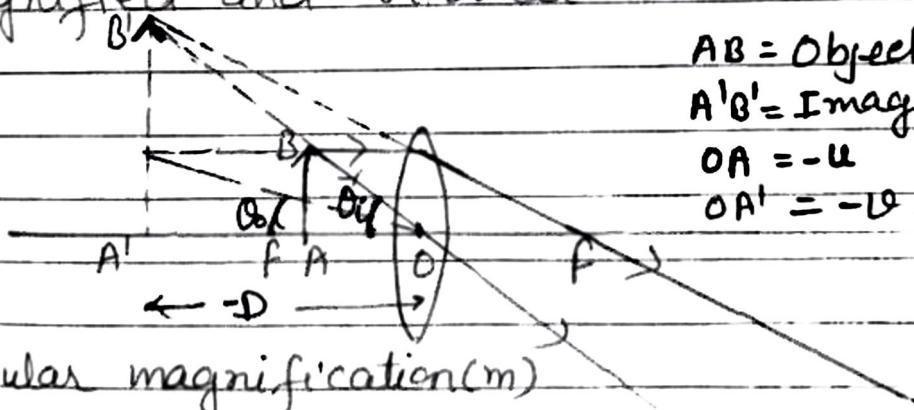
$$\text{Prism} = \frac{\sin(\delta_m + A)}{\sin \frac{A}{2}}$$

## Optical Instruments

The instruments which uses reflecting and refracting properties of mirror, lenses and prism are called optical instruments.  
e.g. Periscope, kaleidoscope, binoculars, telescopes, microscopes etc.

### 1 Simple Microscopes (Magnifying glass):

- \* It is a converging lens of small focal length.
- \* When object is placed b/w focus 'F' and optical centre 'O', the image formed by convex lens is erect, magnified and virtual.



$$AB = \text{Object height}$$

$$A'B' = \text{Image height}$$

$$OA = -u$$

$$OA' = -v = -D$$

Angular magnification ( $m$ )

$$m = \frac{\tan \theta_i}{\tan \theta_o} = \frac{AB/OA}{AB/OA'} \Rightarrow m = \frac{\theta_i}{\theta_o} = \frac{OA'}{OA} \quad \left\{ \begin{array}{l} \text{for large } \\ \text{small } \\ \text{angle} \end{array} \right.$$

or

$$m = \frac{OA'}{OA} = \frac{-D}{-u} = \frac{D}{u}$$

$$\text{by } \frac{1}{f} = \frac{1}{D} - \frac{1}{u} \Rightarrow \frac{1}{f} = \frac{1}{D} - \frac{1}{-u} \Rightarrow \frac{1}{u} = \frac{1}{f} + \frac{1}{D}$$

then

$$m = D \left[ \frac{1}{D} + \frac{1}{f} \right]$$

$$m = D \left[ \frac{1}{v} + \frac{1}{f} \right]$$

Case I - If image is formed at near point (D)  
i.e.  $v = D$

then

$$m = 1 + \frac{D}{f}$$

Case II - If image is formed at infinity (far point) i.e.  $v = \infty$ , then

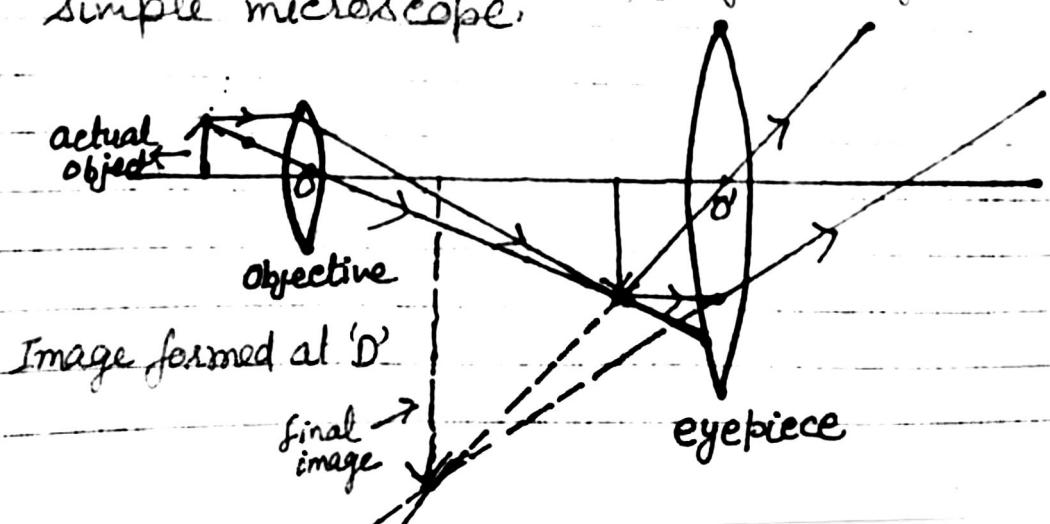
In normal adjustment  $m = \frac{D}{f}$   $[\because \frac{1}{\infty} = 0]$

\* Generally m provided by simple microscope is not more than 9.  $m \leq 9$

### Compound Microscope

In compound microscope two convex lenses are used to increase the magnifying power. One lens is objective lens, which forms real and inverted magnified image.

Image formed by objective lens acts as an object for second lens (Eyepiece) and forms virtual and erect magnifying image like simple microscope.



magnification  $m = m_o m_e$

where,

$m_o \rightarrow$  magnification by objective lens

and  $m_e \rightarrow$  magnification by eyepiece lens

here  $m_o = \frac{v_o}{u_o}$

and  $m_e = \frac{o_i}{o_o} = D \left[ \frac{1}{l_e} + \frac{1}{f_e} \right]$  [for simple microscope]

then

$$m = m_o m_e$$

$$m = \frac{v_o}{u_o} \cdot D \left[ \frac{1}{l_e} + \frac{1}{f_e} \right]$$

\* Length of microscope = Distance b/w objective  
and eyepiece  
 $= v_o + l_e$

\* Case I - If image is formed at near point (at D)

then,  $v = D$

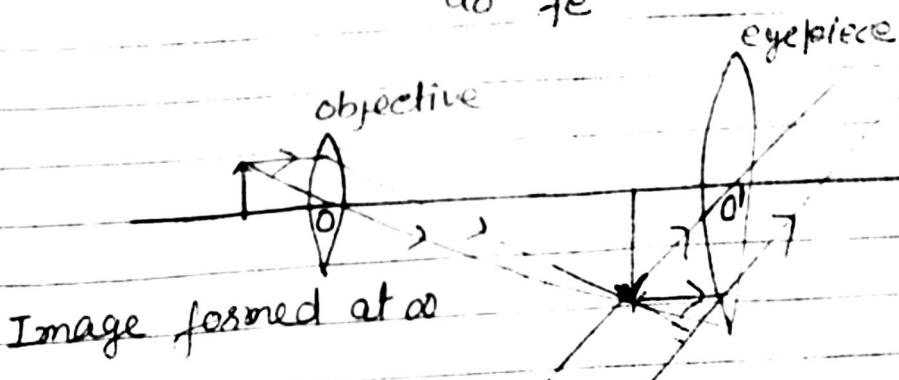
$$m = \frac{v_o}{u_o} \left[ 1 + \frac{D}{f_e} \right]$$

\* Case II

If image is formed at  $\infty$  (far point)

then,  $v_e = \infty$  (Normal Adjustment)

$$m = \frac{v_o}{u_o} \cdot \frac{D}{f_e}$$

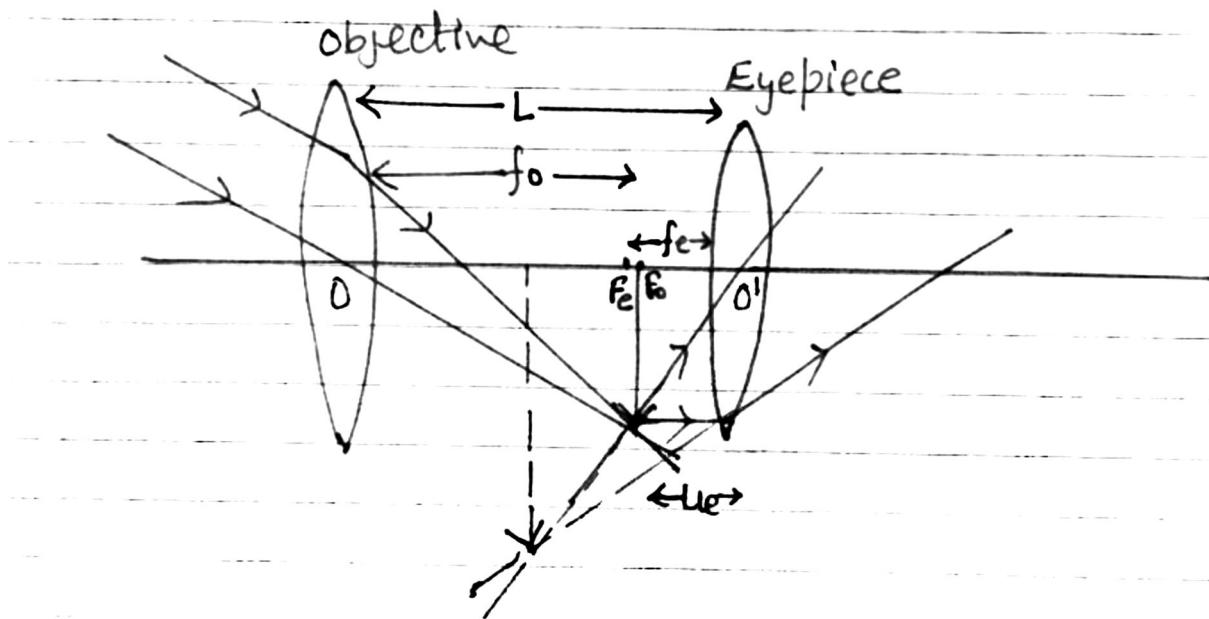


## Astronomical Telescope

It is used to provide angular magnification to distant objects.

It consists two convex lenses - Objective and eyepiece.

- \* Objective has larger focal length and aperture.
- \* Light from distant object enters objective and a real image is formed at focus of objective. Eyepiece then magnifies its image producing a final inverted image.



Case I - Final image is formed at near point (at  $f_e$ )

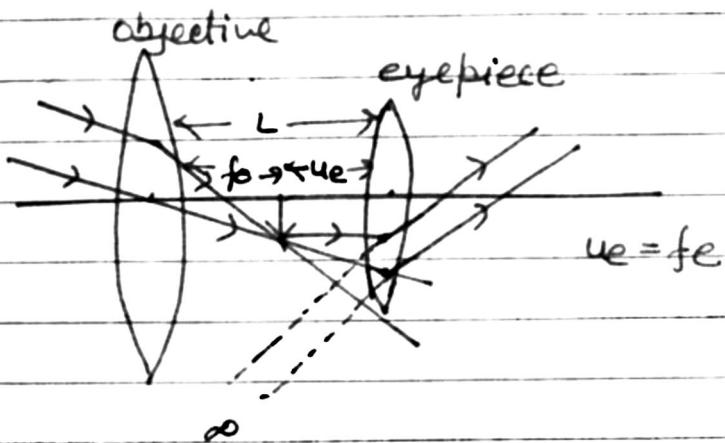
$$m = -\frac{f_o}{f_e} \left[ 1 + \frac{f_e}{d} \right]$$

- \* Length of telescope =  $f_o + u_e = L$

Case II - If final image is formed at far point (at  $\infty$ )  
for image to be at  $\infty$ ,  $u_e = f_e$

$$m = -\frac{f_o}{f_e} \quad [\text{Normal adjustment}]$$

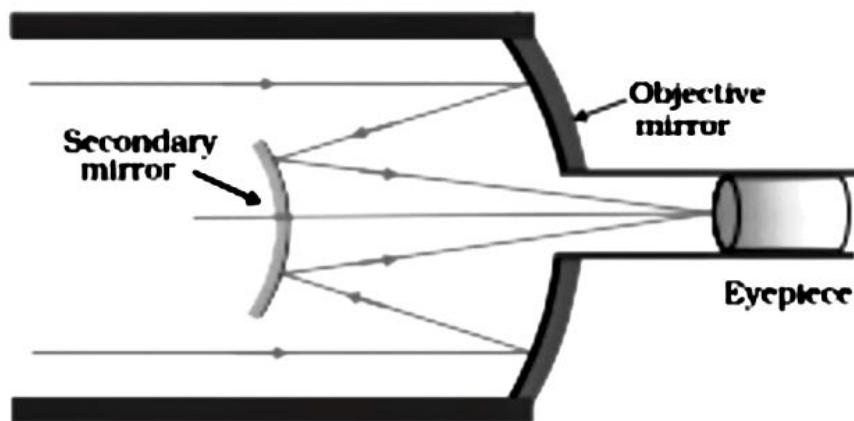
$$L = f_o + f_e \quad [L \rightarrow \text{length of telescope}]$$



- \* Compound microscope is used to observe minute nearby objects whereas the telescope is used to observe distant objects.
- \* In compound microscope focal length of objective is lesser than that of eyepiece but in telescope objective has larger focal length than eyepiece.
- \* The objective of a telescope have large focal length and large aperture to increase the M.P and to collect large amount of light respectively.

# Reflecting type Telescope (Cassegrian telescope)

In such telescope, one objective lens is replaced by a concave parabolic mirror of large aperture, which is free from chromatic and spherical aberrations.



Schematic diagram of a reflecting telescope (Cassegrain).

In normal adjustment, magnifying power

$$m = \frac{f_0}{f_e} = \frac{\frac{R}{2}}{f_e}$$

# **Advantages of Reflecting type telescope**

- 1. There is no chromatic aberration as the objective is a mirror.**
- 2. Spherical aberration is reduced using mirror objective in the form of a parabolic.**
- 3. The image is brighter compared to that in a refracting type telescope.**
- 4. Mirror requires grinding and polishing of only one side.**
- 5. High resolution is achieved by using a mirror of large aperture.**
- 6. A mirror weights much less than a lens of equivalent optical quality.**